SFWR ENG 3DX4 – Assignment 1

1. Consider the following circuit:



Let $R_1 = 40 \ \Omega$, $R_2 = 20 \ \Omega$, $L = 10 \ mH$, and $C = 1 \ \mu F$. The input is v_{in} and the output is v_{out} . Give both the transfer function and a state space representation for the system.

2. A system has state space representation given by:

$$A = \begin{bmatrix} 0 & 1 & 1 \\ 0 & 0 & 1 \\ 8 & -2 & -3 \end{bmatrix},$$
$$B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix},$$
$$C = \begin{bmatrix} 3 & -3 & 0 \end{bmatrix},$$

and D = 0.

- (a) Determine the transfer function for this system.
- (b) Give a different state space representation that yields the same transfer function.
- (c) Give the output response c(t) when the input response r(t) is a unit step function.
- (d) Is the output response stable?